



Removing low-frequency artefacts from Datawell DWR-G4 wave buoy measurements

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Received: 11 September 2015 – Published in Geosci. Instrum. Method. Data Syst. Discuss.: 3 November 2015

Revised: 8 January 2016 – Accepted: 14 January 2016 – Published: 5 February 2016

Abstract. In this study we describe a previously unreported error in the vertical-displacement time series made with GPS-based Datawell DWR-G4 wave buoys and introduce a simple method to correct the resulting wave spectra. The artefact in the time series is found to resemble a sawtooth wave, which produces an erroneous trend following an f^{-2} power law in frequency space. The correction method quantifies the amount of erroneous trend below a certain maximum frequency and removes the spurious energy from all frequencies assuming the above-mentioned f^{-2} power law. The presented correction method is validated against an experimental field test, and its impact on the measured significant wave height is quantified. The method's sensitivity to the choice of the maximum frequency is also briefly discussed.

when compared to an accelerometer-based Datawell Directional Waverider (DWR) (de Vries et al., 2003; Jeans et al., 2003).

The small size of the GPS receiver enables the construction of smaller and more robust wave buoys like the Datawell DWR-G4, which is only 40 cm in diameter. According to our experience these smaller buoys are practical and cost-efficient, especially for short measurements (e.g. Tuomi et al., 2014) where they can be moored or deployed as floating devices.

In this paper we describe an observed error reading in the G4 measurements, suggest an easy and automated corrective method and discuss the accuracy and limitations of the correction based on experiments.

1 Introduction

Surface wind waves are an important factor for the safety and efficiency of marine traffic, seaborne operations and coastal structures. Short-term observations are well suited to map the wave field and to support wave model development, especially at complex shorelines. Currently the large wave buoys utilising accelerometers to measure the pitch, heave and roll of the buoy are considered highly reliable instruments for operational measurements. Nevertheless, there also exist several different technologies that use a GPS receiver to measure the displacement of the wave buoy, which have all been proven to be sufficiently accurate in a majority of situations (Herbers et al., 2012). Especially the technique using the Doppler shift of the GPS signal to measure the velocity of the wave buoy has been shown to produce excellent results

2 The artefact

Although the overall accuracy of the Datawell G4 is not in question, we have observed anomalous behaviour in the vertical-displacement time series calculated on board several different G4 wave buoys over the course of almost a decade. The artefact is large enough to affect the reliability of even robust wave parameters, such as the significant wave height, if no correction is applied. The sawtooth-like artefact in the time series (Fig. 1) cannot be explained by the mooring (e.g. Ashton and Johanning, 2015), as we have also observed similar behaviour with free-floating buoys during measurement campaigns and completely stationary buoys during routine testing. We also rule out instrument failure, since the anomaly has been observed with several individual buoys. We suspect that the source of the artefact might be linked to disturbances in the propagation of the GPS signal that

Table 1. Mean and extreme difference in significant wave height of the G4 wave buoy when compared to the DWR wave buoy. The significant wave height is calculated for both the entire frequency range and for the low-frequency part of the spectra only. Two corrections are made using different maximum frequencies to quantify the erroneous energy. Values are calculated from data where erroneous energy was present (i.e. the correction by the method was at least 0.1 m).

G4 vs. DWR	$\Delta H_s (< 0.1 \text{ Hz})$		ΔH_s	
	mean (m)	extreme (m)	mean (m)	extreme (m)
Uncorrected	0.8	1.8	0.2	0.7
Correction using $f < 0.07 \text{ Hz}$	0.0	0.2	-0.1	-0.5
Correction using $f < 0.04 \text{ Hz}$	0.0	0.3	-0.1	-0.5

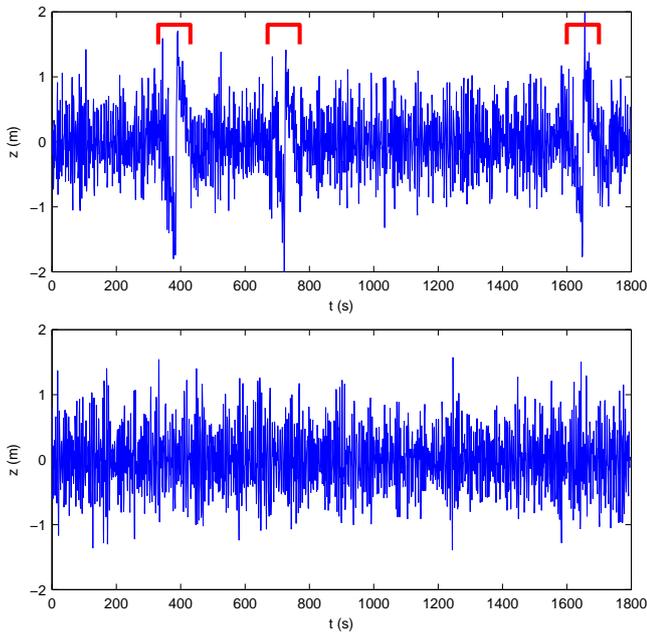


Figure 1. Artefact observed in a G4 buoy. Vertical displacement measured with the G4 buoy with the artificial jumps indicated with red arrows (top panel). Vertical-displacement time series of the measurements by an accelerometer-based DWR made in close proximity and during roughly the same time (bottom panel). The distance between the two devices were about 900 m.

are caused by atmospheric conditions. Even if the receiving unit is functioning properly, any disturbances in the propagation of the signal could lead to an incorrect determination of the velocity of the wave buoy, since the wave buoy relies on the measurement of the Doppler shift. However, we have not found any definite connection between the magnitude of the artefact and any local meteorological parameter (wind speed, humidity etc.).

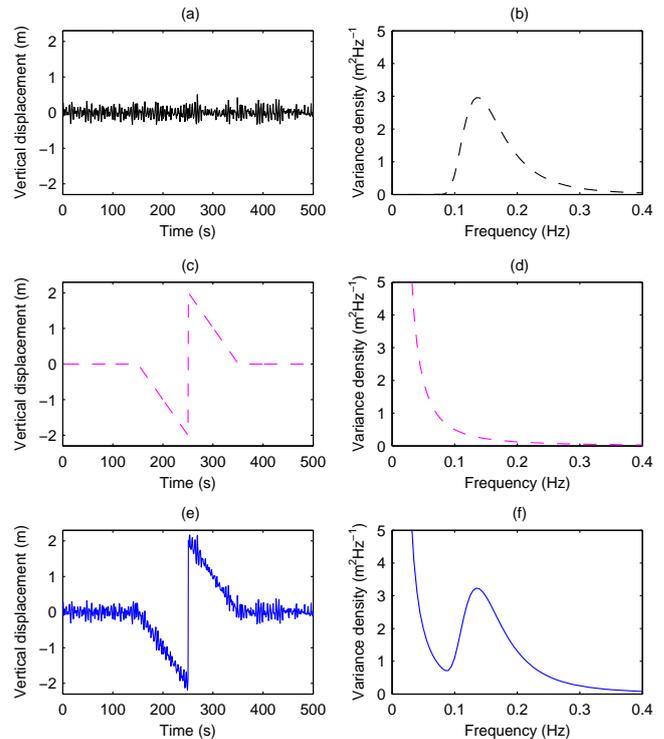


Figure 2. A schematic illustration of signal and the frequency response of a clean time series (a–b), a sawtooth wave (c–d) and the combined time series (e–f). The wave spectrum (f) of the combined signal is just a superimposition of the wave spectra (b, d) of the individual signals.

3 The wave spectrum and the correction method

3.1 The wave spectrum

The irregular nature and frequent occurrence of the anomaly described in Sect. 2 makes manual cleaning both difficult and extremely time consuming. However, the main interest of researchers is usually not the vertical displacement of the buoy, but rather the wave spectrum, which describes the wave field in the frequency domain. Especially the parameters derived from the 1-D spectrum, e.g. the significant wave height and

wave periods, are extensively used both for operational and for research purposes.

The 1-D wave spectrum is the power density spectrum of the vertical displacement. Theoretically it is defined as the Fourier transform of the autocovariance function of the vertical displacement, but in practice it is usually calculated directly from the vertical displacement by using the fast Fourier transform (FFT) (see e.g. Bendat and Piersol, 2010). All the wave spectra in this study are the ones calculated on board the wave buoys by taking the Fourier transform piecewise from the time series, but the correction technique we propose is not dependant on the method used to calculate the wave spectrum. For a more detailed description of the method used on board the buoys the reader is referred to the Datawell manual (Datawell BV, 2014).

A schematic illustration of the frequency responses of the relevant signals is shown in Fig. 2. The power density spectrum of a sawtooth wave follows an f^{-2} frequency power law, which is not limited by any upper frequency. Solutions depending on discarding all data from the spectra below a cut-off frequency will therefore not be sufficient, even though it has previously been used to remove erroneous low-frequency data of a different type (Joodaki et al., 2013).

The observed error reading in Fig. 1 has the shape of a sawtooth wave. The correction method presented in this paper will therefore be based on the known frequency response of the artefact.

3.2 The correction method

To quantify the amount of spurious energy, we will first need to determine a frequency interval that we can assume to contain pure erroneous trend. As a first guess for the upper limit we took 0.07 Hz. This choice was based on our long experience that there is practically no physically meaningful wave data below that frequency in the Baltic Sea (e.g. Kahma, 1981; Kahma et al., 2003; Pettersson, 2004; Tuomi, 2008; Tuomi et al., 2011). For the purpose of our calculations we can therefore assume that frequencies below 0.07 Hz contain only pure erroneous trend. The choice of frequency interval for e.g. a different geographical location will have to be made based on the knowledge of the local wave field. The effect the chosen maximum frequency has on our results is further discussed in Sect. 5.

Because of the underlying f^{-2} power law the erroneous trend will have a constant value if the spectrum is scaled by a factor of f^2 . We will then calculate the mean value of the scaled trend from frequencies below 0.07 Hz and remove it from the entire spectrum prior to de-scaling. A schematic picture of the de-trending process is shown in Fig. 3.

In practice the trend will not always be smooth. The variations around the mean value may cause small positive and negative residuals even below the chosen maximum frequency of 0.07 Hz. As an additional step, we will remove any residuals below 0.07 Hz (usually very small) and set possible

negative values to zero (because the original spectral file is always strictly non-negative). The first step is mostly cosmetic and the latter practical. We want to stress that the real correction of the spectrum is made by the removing of the mean trend.

4 Experimental

We at the Finnish Meteorological Institute¹ (FMI) have observed waves in the Baltic Sea since the 1970s both campaign-based (e.g. Kahma, 1981; Pettersson, 2004; Tuomi et al., 2014) and operationally (e.g. Pettersson and Jöns-son, 2004; Tuomi, 2008). The measurements have been conducted with various instruments, including wave buoys, acoustic Doppler current profilers (ADCPs) and wave staffs. Our operational measurements are made with wave buoys equipped with accelerometer-based sensors, but we have also used GPS-based wave buoys for additional shorter measurements since 2006.

To test the correction method described in Sect. 3, we deployed a GPS-based Datawell DWR-G4 (henceforth, “the G4”) in close proximity to FMI’s operational accelerometer-based Directional Waverider (“the DWR”) in the centre of the Gulf of Finland (Fig. 4). The measurement period for the G4 was 4–20 May 2015, during which time the significant wave height measured by the DWR ranged from 0.1 to 2.9 m.

Both wave buoys use a 0.78 s sampling time to measure the 1600 s time series from which they calculate the wave spectra every half hour. The spectra from both buoys have a frequency range of 0.025–0.580 Hz with a resolution of 0.01 Hz (0.005 Hz for frequencies under 0.1 Hz).

The significant wave height is defined as $H_s = 4\sqrt{m_0}$, where m_0 is the zeroth moment (i.e. the integral) of the wave spectrum. The integral of the wave spectrum is also the variance of the vertical-displacement time series.

5 Results

The variance density (m^2Hz^{-1}) of each frequency bin from the G4 wave buoy was compared to those of the DWR for the whole data set. Figure 5 shows the bias of the original and corrected G4 spectra compared to the reference data from the DWR. We can see that the original G4 data have a positive bias following the expected f^{-2} power law, which is no longer visible after the correction. The correction method applied to the, presumably correct, DWR spectra resulted in only negligible changes (not shown).

The maximum reduction in significant wave height when using the correction method was 1.0 m (a reduction from 3.3 to 2.3 m). To visualise the occurrence frequency of the anomaly in our field data, we plotted the difference in significant wave height from the G4 buoy before and after the use

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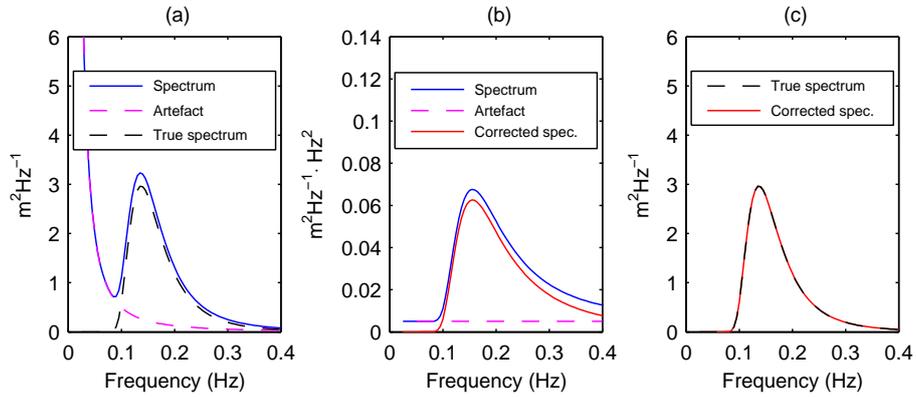


Figure 3. A schematic illustration of the approach to correct a wave spectrum with erroneous trend. A hypothetical spectrum containing erroneous low-frequency energy is shown in (a). The method scales the spectrum by multiplication of f^2 to reveal the power law of the erroneous trend (b). The level of the trend (dashed magenta) is determined from the low frequencies where the scaled spectrum is constant, and the trend is removed from all frequencies. The de-scaled spectrum is shown in (c).

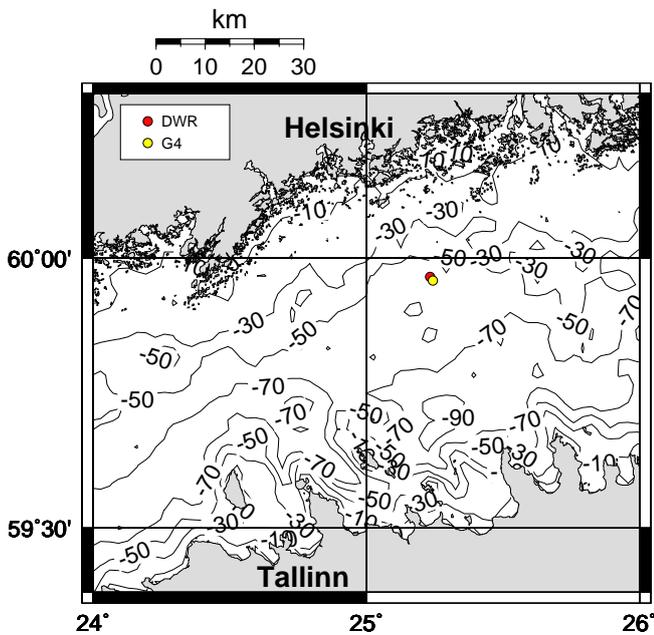


Figure 4. The location of the deployed wave buoys in the Gulf of Finland. The operational DWR (red circle) is anchored at a depth of 62 m at 59°57.90' N, 025°14.11' E. The G4 (yellow circle) was anchored at a similar depth at 59°57.50' N, 025°14.57' E.

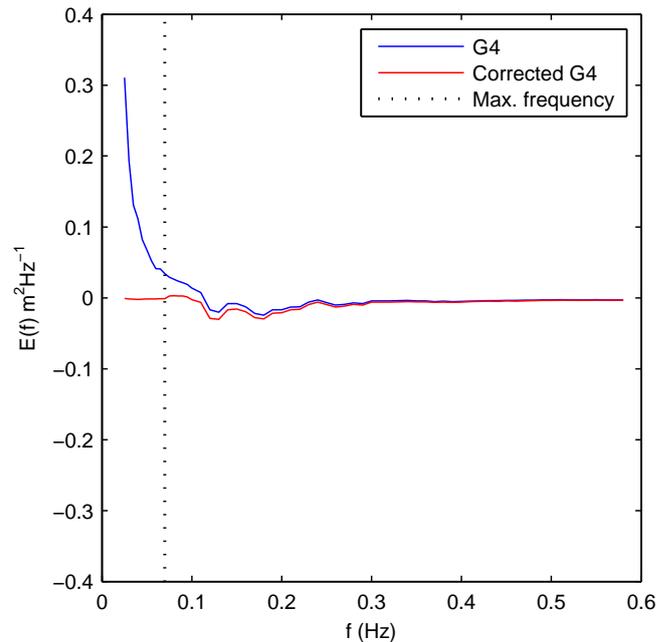


Figure 5. Bias of the power spectrum of the G4 data before and after the correction compared to the reference data from the DWR. The distribution is based on 3 weeks of data.

of the correction method in a logarithmic histogram (Fig. 6). The relative value is defined as the difference between the original and corrected significant wave height normalised by the original significant wave height.

Four situations with an increasing amount of erroneous trend are shown in Fig. 7. The first case (a) illustrates that the method does not interfere with an uncorrupted spectrum. In the three following cases the erroneous trend continues above the maximum frequency used to quantify the spurious

energy (0.07 Hz), but even these higher frequencies are corrected as a comparison to the DWR spectra reveals.

In addition to errors in the significant wave height the artefact will also lead to unphysical values if the peak period (i.e. the period containing the most energy) is calculated for situations resembling that of Fig. 7d. This must be taken into account especially in operational applications, but the data need not be discarded if a proper automated correction method is used.

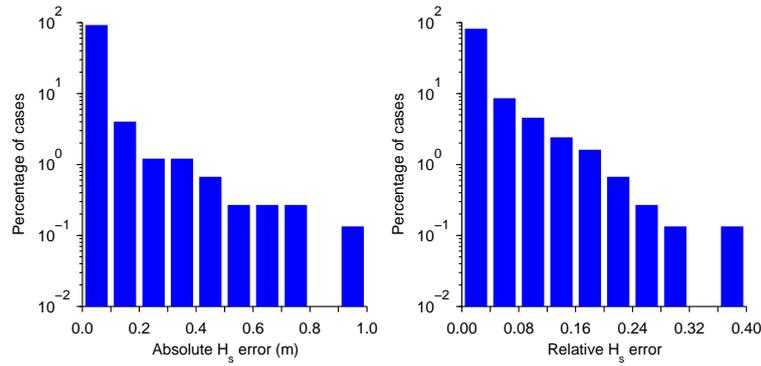


Figure 6. The difference in significant wave height when calculated from the original and corrected wave spectra measured by the G4 wave buoy. Absolute values (left panel) and relative values (right panel). The relative value is the difference between the original and corrected significant wave height normalised by the original significant wave height.

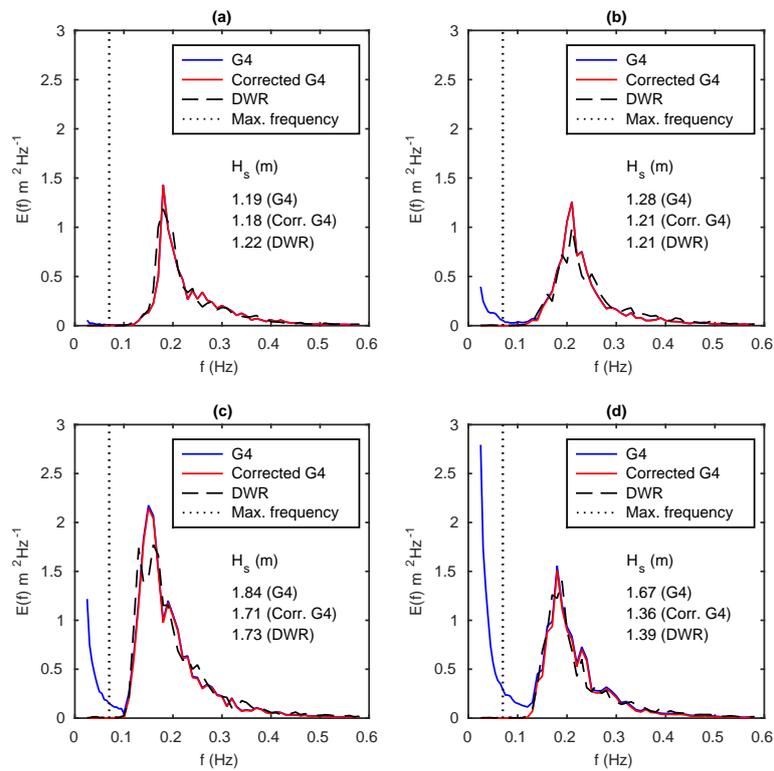


Figure 7. The power law method applied to four example wave spectra from May 2015 with different amount of erroneous trend present. The significant wave height H_s is calculated for the original G4 data, the corrected G4 data and the DWR data.

Because of the small size of the Baltic Sea, we were able to use a relatively high maximum frequency of 0.07 Hz (i.e. 14 s wave period) as an initial guess for an appropriate value. However, one cannot generally assume that there are no physically relevant wave data below 0.07 Hz, which calls for a lower upper limit when quantifying the trend. To test the sensitivity of the method, we repeated the calculations using a maximum frequency of 0.04 Hz (i.e. 25 s wave period).

The results in Table 1 show the difference in significant wave height between the G4 and the DWR wave buoys when using the different frequency intervals. We calculated the values using only the data when erroneous trend was observed, which we defined somewhat arbitrarily as cases when the correction of the significant wave height to the G4 wave buoy was at least 0.1 m. The results show that the proposed method is insensitive to the choice of the maximum frequency. This

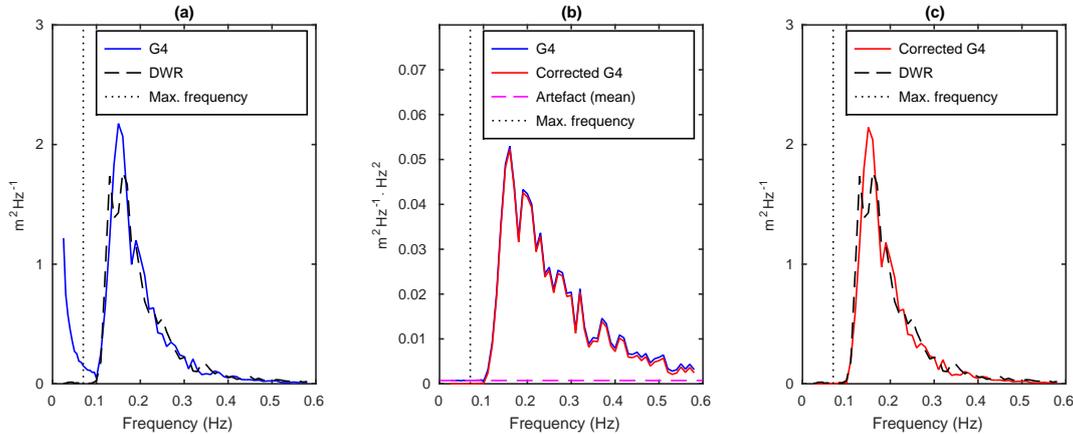


Figure 8. An example of the correction applied to a wave spectrum from a G4 wave buoy (14 May 2015). The original spectrum (a), the spectrum scaled by f^2 and the level of the mean trend (b) and the corrected de-scaled spectrum (c). The spectrum from the DWR is shown for comparison. The dotted line indicates the maximum frequency (0.07 Hz) used to determine the level of the erroneous trend.

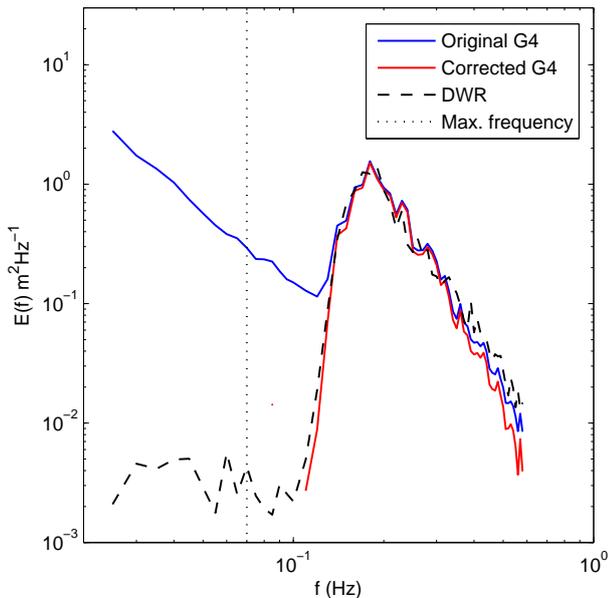


Figure 9. The example spectra from Fig. 7d shown on a logarithmic scale for illustrative purposes. Note that the values that are in set to zero in the corrected spectra cannot be displayed on the logarithmic scale.

is easily explained by the fact that the level of the trend is equally well defined below 0.04 Hz (Fig. 8b).

To better illustrate even the small differences between the original and corrected spectra, we plotted the already-presented case of Fig. 7d on a logarithmic scale (Fig. 9). A trend following an f^{-2} power law should be linear in a logarithmic plot, which is indeed the case. The figure also illustrates that a slight overcorrection is possible for the highest frequencies (0.40–0.58 Hz), where the trend becomes the same order of magnitude as the spectrum. This can be due to

other small low-frequency errors that contribute to the spectrum below 0.07 Hz, which in turn will make the correction slightly too large. However, this possible overcorrection is inconsequential for the calculation of any basic parameters, such as the significant wave height. Even though we recommend the corrected data to be carefully checked when used in advanced wave studies, the method presented in this paper is suitable to be implemented as an automated approach for e.g. operational applications.

6 Conclusions

In this paper we introduce a simple automated method to correct Datawell DWR-G4 data for an error observed in the lower frequencies. This error is caused by a sawtooth-like artefact in the time domain and thus follows an f^{-2} power law in the frequency domain (Figs. 1 and 2). We have concluded that the artefact in the time domain is caused by the use of the Doppler shift technology, but we are not aware of any previous reports of this kind of behaviour.

The basic idea of the method is to calculate the level of the erroneous trend from the frequency bins we know to lack physically relevant information (we used 0.07 Hz as an upper limit for the Baltic Sea) and then remove it for the whole frequency range (see Fig. 3 for a schematic overview of the method).

We compared the original and corrected spectra to reference spectra made with an accelerometer-based Datawell Directional Waverider moored 900 m away. The corrected spectra match the reference spectra better than the original ones for the lower frequencies. In addition, the excess erroneous energy in the spectra is removed also above the chosen maximum frequency of 0.07 Hz (Fig. 7). The comparison in Table 1 shows that the power law method increases the accu-

racy of the observations even if only integrated parameters, such as significant wave height, are considered.

The results presented in Table 1 show that the method produces the same results if the level of the erroneous trend is quantified only below 0.04 Hz. This robustness increases the usability of the correction method for different physical and geographical conditions.

Although the correction is generally concentrated on the low-frequency part of the spectrum, there is a possibility of a small overcorrection of the high-frequency tail (> 0.4 Hz) (Fig. 9). Luckily, these minor differences are not important for basic applications that use only integrated parameters. Nonetheless, the corrected data should be analysed if they are to be used for more advanced wave research.

Data availability

The spectral files of both the wave buoys for the study period and the MATLAB code found in Appendix A are available as a supplement.

Appendix A: Code for correcting wave buoy spectra

A simple MATLAB code for correcting data from Datawell G4 wave buoys.

```
function S_DT=detrend_wavespec(f,S,f_max)

S_scaled=S.*f.^2; % Scale the spectrum with f^2

bin_max=find(f<=f_max,1,'last'); % Select the bins used to

                                % calculate the trend

Trend=mean(S_scaled(1:bin_max)); % Calculate mean scaled trend

S_scaled=S_scaled-Trend; % Remove mean scaled trend

S_scaled(1:bin_max)=0; % These freq. bins did not contain any

                                % real information

S_scaled=max(S_scaled,0); % Force to positive values

S_DT=S_scaled./f.^2; % Return the de-scaled spectrum
```

The Supplement related to this article is available online at doi:10.5194/gi-5-17-2016-supplement.

Acknowledgements. We are grateful to senior scientist Kristian Spilling from the Finnish Environment Institute for arranging the time for our measurements during his cruise on RV *Aranda* on such short notice.

Edited by: C. Waldmann

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